

**Name:**

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**Directions:** Complete all question and **show all applicable work.** Partial credit will be given. All questions are equally weighted.

1.) Calculate the derivative for each of the following.

(a)  $2x^3 + 3x^2 + 5x + 23$

(b)  $e^x \sin(x)$

2.) Calculate the derivative for each of the following.

(a)  $\frac{1}{3} \ln(x^3)$

(b)  $\arcsin(\sqrt{1 - x^2})$

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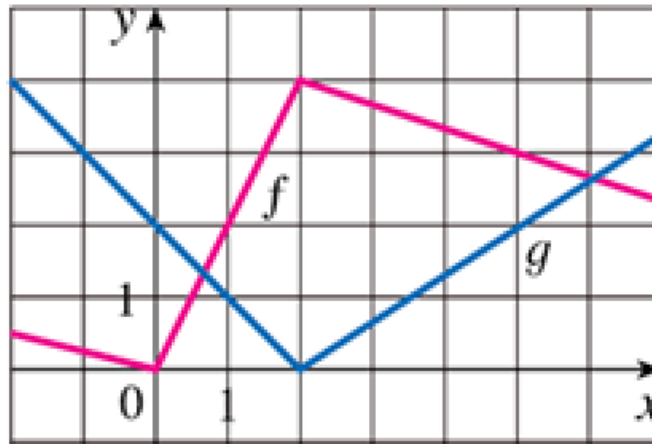
3.) Given  $y^2 + 2xy = 2x^2$ , calculate  $\frac{dy}{dx}$ .

4.) Find a linear approximation to  $f(x) = e^x$  at  $x = 0$ .

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5.) Compute:  $\sin\left(\arctan\left(\frac{3}{4}\right)\right)$

6.) Using the graph below, let  $F(x) = f(g(x))$ , find  $F'(1)$ .



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- 7.) A ball is thrown straight up into the air with its height given by  $h = -4.9t^2 + 20t + 3$ .
- (a) Find the velocity of the ball for any time  $t$ .
  - (b) Find the acceleration of ball for any time  $t$ .
  - (c) When does the ball reach its peak height?
  - (d) What is the peak height?

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8.) BONUS (5pts): Using the derivatives of  $\sin(x)$  and  $\cos(x)$ , prove that

$$\frac{d}{dx} \tan(x) = \sec^2(x).$$